

# Model-based Policy Gradients with Entropy Exploration through Sampling

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## Summary

- We relax the analytic gradients constraint of PILCO [1] by using reparameterized trajectory samples to estimate expected costs.
- Our sampling approach allows gradient-based optimization of arbitrary differentiable cost functions without requiring complex analytic calculations.
- We introduce two different regularization terms to encourage policy exploration by maximizing entropy and minimizing reward variance.

## Gaussian Process Dynamics Models

Given a deterministic environment with transition function  $f$  with continuous states  $\mathbf{s} \in \mathbb{R}^D$  and actions  $\mathbf{a} \in \mathbb{R}^F$ , we model  $f$  using a Gaussian process

$$p(\mathbf{s}_{t+1} | \mathbf{x}_t) := \mathcal{GP}(\mathbf{s}_t, k(\mathbf{x}_t, \mathbf{x}'_t))$$

where  $\mathbf{x}_t = (\mathbf{s}_t, \mathbf{a}_t) \in \mathbb{R}^{D+F}$  and each dimension of the GP is independent conditioned on  $\mathbf{x}_t$ .

## Trajectory Sampling

Given a starting distribution  $p(\mathbf{s}_0)$  and a deterministic policy  $\pi(\cdot | \theta)$ , we ancestral sample trajectories  $\tau = (\mathbf{s}_0, \dots, \mathbf{s}_T)$  from the joint distribution  $p(\tau) = p(\mathbf{s}_0)p(\mathbf{s}_1 | \mathbf{s}_0, \mathbf{a}_0) \dots p(\mathbf{s}_T | \mathbf{s}_{T-1}, \mathbf{a}_{T-1})$  where  $\mathbf{a}_t = \pi(\mathbf{s}_t | \theta)$  and Monte Carlo estimate the expected reward under dynamics model  $p$  using  $N$  trajectory samples

$$J(\theta) = \mathbb{E}_\tau[r(\tau)] \approx \sum_{i=1}^N \sum_{t=1}^T r(\mathbf{s}_t^{(i)}, \mathbf{a}_t^{(i)}) \quad (1)$$

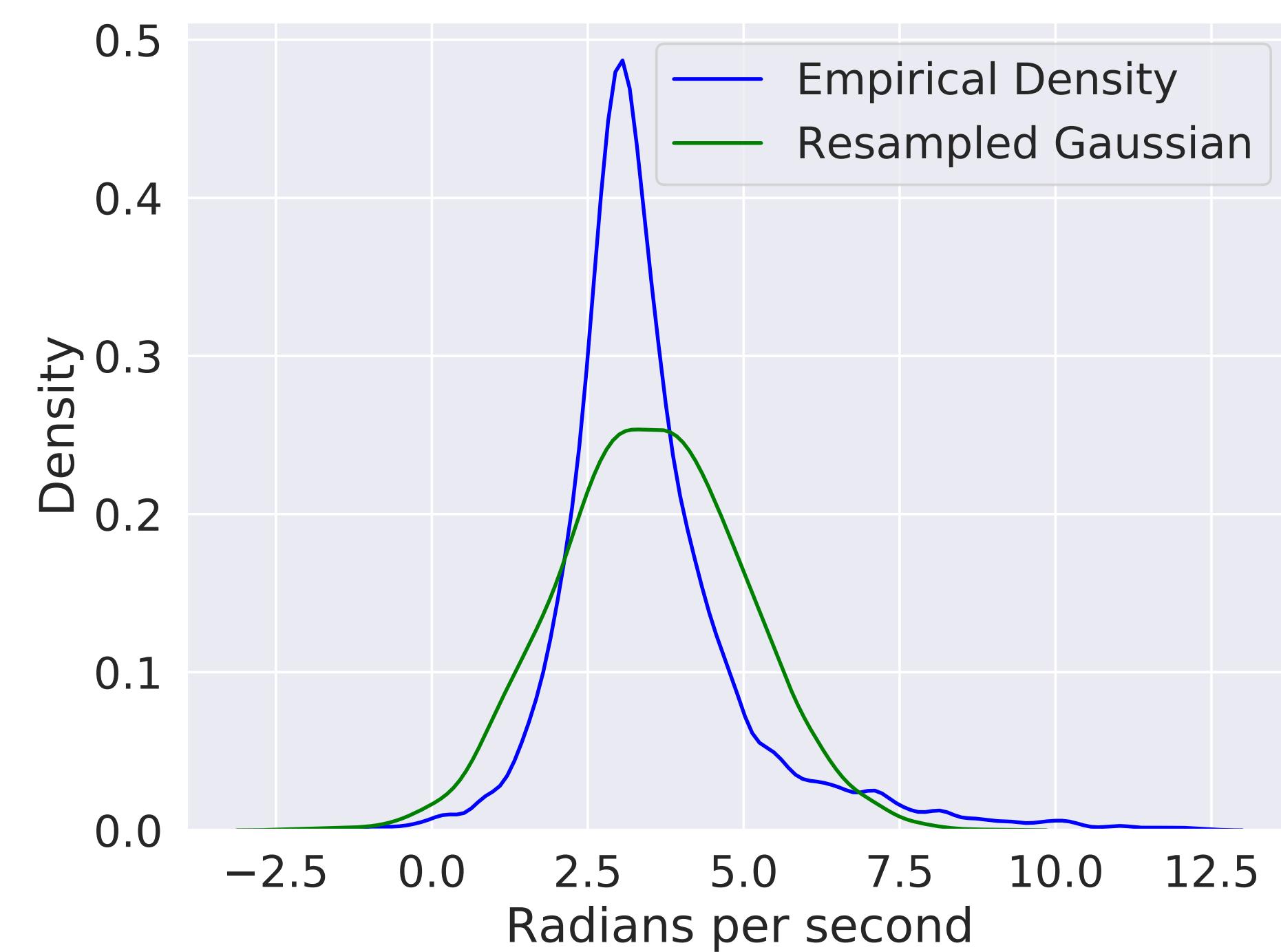


Figure 1: An example of the non-Gaussian marginal distribution of the pole velocity at  $T = 30$  estimated using trajectory sampling and Gaussian resampling [2]

## Algorithm

**Input:** Starting distribution  $p(\mathbf{s}_0)$ , initial policy  $\pi(\cdot | \theta)$   
Initialize dataset  $\mathcal{D}$  by applying a random actions to environment  
**for** episode = 1, ...,  $M$  **do**  
    Learn GP dynamics model using  $\mathcal{D}$   
    Gradient-based optimization of  $J(\theta)$  (1) by sampling trajectories  
    Apply  $\pi(\cdot | \theta)$  to environment, add observations to  $\mathcal{D}$   
**end for**  
**Output:**  $\pi(\cdot | \theta)$

## Incentivizing Exploration

We explore the effects of two additional terms to the objective function to encourage exploration:

- Variance: maximize  $J(\theta) - \frac{1}{N-1} \sum_{i=1}^N \left[ \sum_{t=1}^T r(\mathbf{s}_t^{(i)}, \mathbf{a}_t^{(i)}) - J(\theta) \right]^2$
  - Entropy: maximize  $J(\theta) + \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^T \left[ \frac{1}{2} \sum_{d=1}^D \log(\sigma_t^{(i)})_d^2 \right]$
- where  $(\sigma_t^{(i)})_d^2$  is the variance of the  $d^{\text{th}}$  dimension of  $p(\mathbf{s}_{t+1} | \mathbf{x}_t)$ .

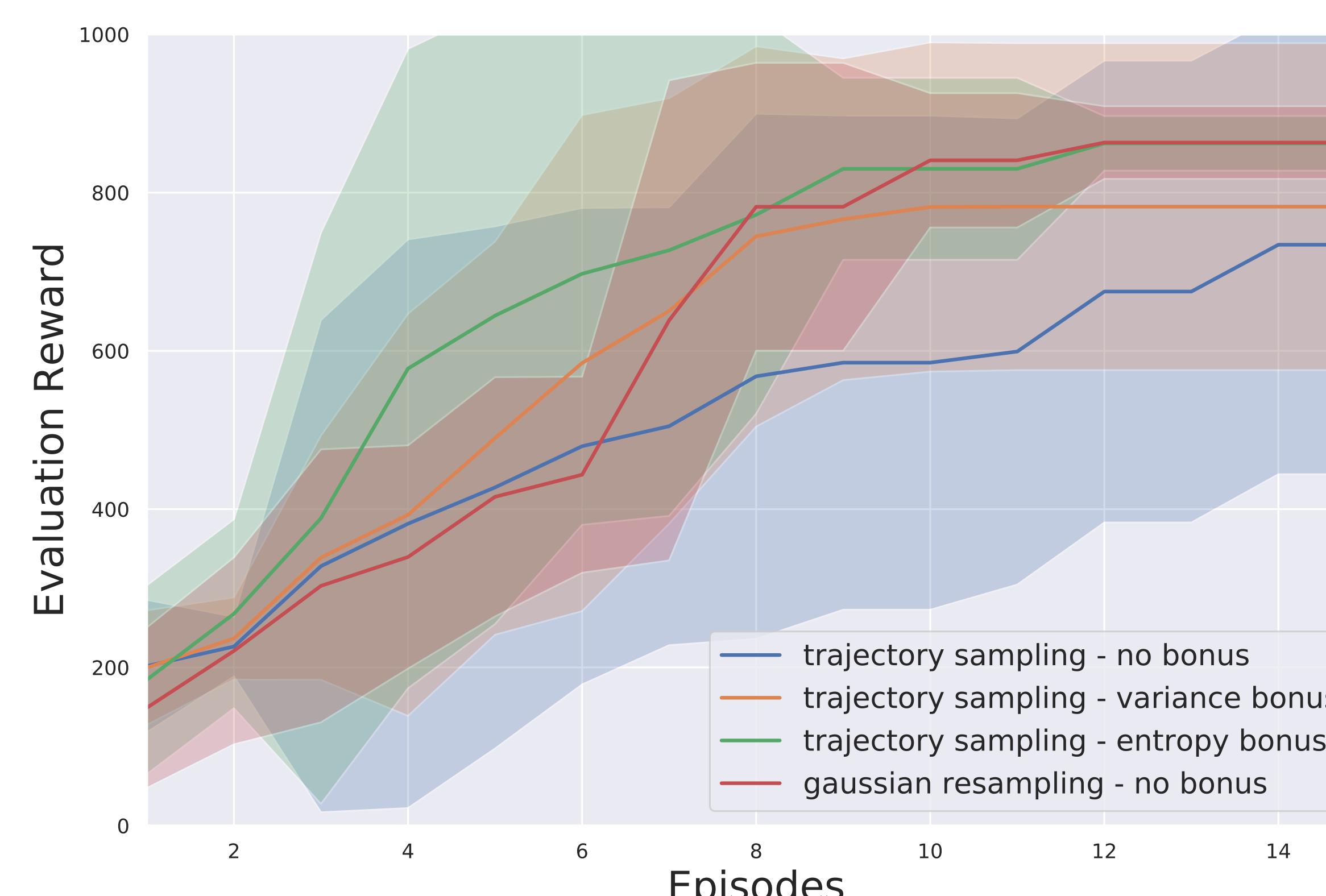


Figure 2: The reward curves for each method evaluated on the Deepmind Control Suite [3] cartpole swingup task averaged over 6 trials with 90% confidence intervals using  $N = 256$  samples

Figure 2 shows that entropy and variance terms improve the reliability of trajectory sampling. Note that Gaussian resampling and trajectory sampling reproduce the sample efficiency from [1].

## Advantages of Trajectory Sampling

- With trajectory sampling and automatic differentiation, we can use *any* differentiable cost function.
- We no longer need to make moment matching approximations or to manually derive

$$\frac{dJ}{d\theta} = \sum_{t=1}^T \frac{d\mathbb{E}_{\mathbf{x}_t}[r(\mathbf{x}_t)]}{d\theta}$$
$$\frac{d\mathbb{E}_{\mathbf{x}_t}[r(\mathbf{x}_t)]}{d\theta} = \frac{\partial \mathbb{E}_{\mathbf{x}_t}[r(\mathbf{x}_t)]}{\partial \mu_t} \frac{d\mu_t}{d\theta} + \frac{\partial \mathbb{E}_{\mathbf{x}_t}[r(\mathbf{x}_t)]}{\partial \Sigma_t} \frac{d\Sigma_t}{d\theta}$$

etc...

as done in [1]. Instead, we can instead simply sample from the model trajectory distribution with:

```
import torch
import gpytorch
...
def reward(states):
    ...
states = sampling_procedure(initial_dist)
obj = reward(states)
obj.backward()
```

## References

- [1] Marc Peter Deisenroth, Dieter Fox, and Carl Edward Rasmussen. Gaussian processes for data-efficient learning in robotics and control. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 37(2):408–423, 2015.
- [2] Paavo Pirmas, Carl Edward Rasmussen, Jan Peters, and Kenji Doya. PIPPS: Flexible model-based policy search robust to the curse of chaos. In *Proceedings of the 35th International Conference on Machine Learning*, volume 80 of *Proceedings of Machine Learning Research*, pages 4065–4074, Stockholm, Sweden, 10–15 Jul 2018. PMLR.
- [3] Yuval Tassa, Yotam Doron, Alistair Muldal, Tom Erez, Yazhe Li, Diego de Las Casas, David Budden, Abbas Abdolmaleki, Josh Merel, Andrew Lefrancq, et al. Deepmind control suite. *arXiv preprint arXiv:1801.00690*, 2018.

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